## White Station High School

## Algebra 2 Summer Work Packet

This set of problems contains math concepts from Algebra 1 and/or Geometry that are important prerequisite skills for Algebra 2. WSHS is requiring all students who are enrolled in Algebra 2 for the 2022-2023 school year to turn in a **completed packet** on **Monday, August 8, 2022** which *will be graded* by your Algebra 2 teacher. This is the first day of the school year. In the following pages, there are <u>43 required</u> <u>problems</u> with examples to guide you through each concept. After these 43 problems, there are additional problems that are OPTIONAL but will provide further practice for each of the concepts.

This packet does NOT need to be printed. Students are not expected to write on it. ALL problems are to be worked out by hand on notebook paper. Please keep the problems in order by number, writing down the problem numbers as you work through it. When working the problems, students should NOT use a calculator, and must show the mathematical steps in detail in order to receive credit.

If you experience difficulty working through this packet, we recommend you utilize the following free websites:

- https://www.khanacademy.org/signup
- https://www.teachertube.com/categories/math
- <a href="http://www.algebralab.org/studyaids/studyaid.aspx">http://www.algebralab.org/studyaids/studyaid.aspx</a>
- https://www.purplemath.com/modules/index.htm

Students will benefit most from this work by starting it early. You should try to complete a problem each day, as if it were a daily practice assignment. Do **NOT** do all of it at one time. You are more likely to retain the information if it is spread out as a review throughout the summer. Algebra 2 is a challenging class, and you will need these prerequisite skills as you enter the class to be successful. As you prepare, remember that there will be a test during the first week of school over these concepts.

For students who want a more thorough review of Algebra 1 or advanced look into Algebra 2, please create an account at <a href="https://www.khanacademy.org/signup">https://www.khanacademy.org/signup</a> Please enter a "coach" code of 5B9ASA for Algebra 1 and a code of JRSR4T for Algebra 2.

During the school year, students will learn to use the TI NSPIRE CX calculator. If you are planning to purchase a calculator for the 2022-2023 school year, note that these are calculators used in the classrooms and on state testing. There will be class sets of these calculators available specifically for classroom use.

We are excited about working with you in this upcoming school year. We want all students to feel prepared and confident throughout Algebra 2, and these concepts will set you up for that kind of success.

Sincerely,

Carrye Holland, Principal WSHS Math Department

## Summer Work 22-23

Solve each equation for the variable (Use the following examples to guide you).

Solve: 3 ½ p = 1 ½		Solve: -5n = 60	Original equation
$\frac{7}{2}p = \frac{3}{2}$	Original equation	<u>-5n</u> = <u>60</u> -5 -5	Divide both sides by -5 or multiply both sides by -1/5
-	Rewrite each mixed number as an improper fraction	n = -12	Simplify
$\frac{2}{7} \left( \frac{7}{2} p \right) = \left( \frac{3}{2} \right) \frac{2}{7}$	Multiply each side by the reciprocal of 7/2.	Check: -5 (-12) = 60 60 = 60	Substitute solution for variable Left Hand Side = Right Hand
$p = \frac{3}{7}$	Simplify		Side LHS = RHS correct
Check: $3 \frac{1}{2} \left(\frac{3}{7}\right) = 1 \frac{1}{2}$	Substitute solution for variable		
$\frac{7}{2}\left(\frac{3}{7}\right) = \frac{3}{2}  .$	Rewrite each mixed number as an improper fraction		8
$\frac{3}{7} = \frac{3}{7}$	Left Hand Side = Right Hand , Side LHS = RHS correct		

Example 1	Example 2	Example 3
Solve: $5y - 8 = 3y + 12$	Solve: $-11 - 3y = 8y + 1$	Solve: $4(2a-1) = -10(a-5)$
5y - 8 - 3y = 3y + 12 - 3y	-11-3y+3y=8y+1+3y	8a-4=-10a+50
2y - 8 = 12	-11 = 11y + 1	8a - 4 + 10a = -10 a + 50 + 10a
2y - 8 + 8 = 12 + 8	-11 - 1 = 11y + 1 - 1	18a - 4 = 50
2v = 20	-12 = 11y	1 8a - 4 + 4 = 50 + 4
$2\mathbf{v} = 20$	-12 = 11y	18a = 54
$\frac{2}{2}$	11 11	18a = 54
y = 10	<u>-12</u> = y	18 18
3	111	a = 3
Check: $5y - 8 = 3y + 12$	1	
5(10) - 8 = 3(10) + 12	$-1\frac{1}{11} = y$	Check: $4(2a-1) = -10(a-5)$
50 - 8 = 30 + 12		4(2(3)-1)=-10(3-5)
42 = 42	Check: $-11 - 3y = 8y + 1$	4(6-1)=-10(-2)
LHS = RHS correct	$-11-3\left(\frac{-12}{11}\right)=8\left(\frac{-12}{11}\right)+1$	4 (5) = 20 20 = 20
	36 -96	LHS = RHS correct
	$-11 + \frac{36}{11} = \frac{-96}{11} + 1$	
	11 11	
	$\frac{-121}{+} + \frac{36}{-} = \frac{-96}{+} + \frac{11}{-}$	
	11 11 11 11	-
	-8585	
a	11 11	
20	LHS = RHS correct	

1. 
$$20 = y - 8$$

2. 
$$-17 = b + 4$$

3. 
$$\frac{1}{5}p = \frac{3}{5}$$

4. 
$$-3t = 51$$

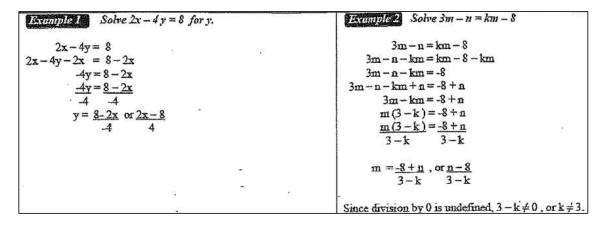
5. 
$$5x + 2 = 2x - 10$$

**6.** 
$$4.4s + 6.2s = 8.8s - 1.8$$

7. 
$$8 - 5p = 4p - 1$$

8. 
$$3(a+1)-5=3a-2$$

Solve each equation or formula for the indicated variable. (Use the following examples to guide you).



**9.** Solve (x + f) + 2 = j for x.

**10.** Solve 7x + 3y = m for y.

Write an equation for the function, in function notation. Then complete the table. (Use the following example to guide you).

Example: Suppose you purchased a number of packages of blank CDs. If each package contains 3 CDs, you could make a chart to show the relationship between the number of packages of compact disks and the number of disks purchased. Use x for the number of packages and y for the number of compact disks.

Make a table of ordered pairs for several points of the graph.

Number of	1	2	3	4	5
Number of CDs	3	6	9	12	15

The difference in the x values is 1, and the difference in the y values is 3. This pattern shows that y is always three times x. This suggests the relation y = 3x. Since the relation is also a function, we can write the equation in functional notation as f(x) = 3x.

11.

х	-2	-1	0	1	2
У	10	7	4		

Write an equation of the line in standard form with the information given. (Use the following examples to guide you).

Example 1: Write an equation of a line in standard form whose slope is -4 and whose y-intercept is 3.

$$y = mx + b$$
 $y = -4x + 3$ 
 $+4x + 4x$ 
 $4x + y = 3$ 

Example 2: Graph  $3x - 4y = 8$ 
 $3x - 4y = 8$ 
 $-4y = -3x + 8$ 
 $-4y = -3x + 8$ 

Original equation

 $-4y = -3x + 8$ 

Divide each side by -4

 $y = \frac{3}{4}x - 2$ 

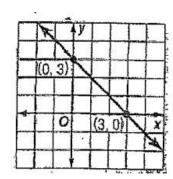
Simplify

Simplify

The y-intercept of y = 3/4x - 2 is -2 and the slope is  $\frac{1}{4}$ . So graph the point (0, -2). From this point, move up 3 units and right 4 units. Draw a line passing through both points.

Standard Form	Ax + By = C .
Slope-Intercept Form	y = mx + b, where m is the given slope and b is the y-intercept
	The state of the s
Point-Slope Form	$y-y_1=m(x-x_1)$ , where m is the given slope and $(x_1,y_1)$ is the given point

- 12. Slope 8 and y-intercept -3
- 13.



**14.** Graph the equation 2x - y = -1

Graph each system of equations. Then determine whether the system has no solution, one solution, or infinitely many solutions. If the system has one solution, tell what it is. (Use the following examples to guide you).

Example: Graph each system of equations. Then determine whether the system has no solution, one solution, or infinitely many solutions. If the system has one solution, name it.

$$x - y = 4$$

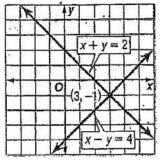
The graphs intersect. Therefore, there is one solution. The point (3, -1) seems to lie on both lines. Check this estimate by replacing x with 3 and y with -1 in each equation.

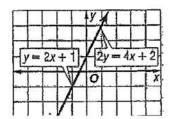
$$x+y=2$$
.  
 $3+(-1)=2$   
 $x-y=4$   
 $3-(-1)=3+1 \text{ or } 4$ 

The solution is (3,-1).

$$2y = 4x + 2$$

The graphs coincide. Therefore there are infinitely many solutions.





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15. 
$$\begin{cases} y = -2 \\ 3x - y = -1 \end{cases}$$

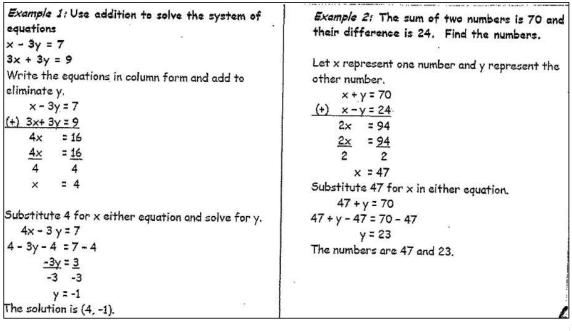
**16.** 
$$\begin{cases} 2x + y = 6 \\ 2x - y = -2 \end{cases}$$

Use substitution to solve the system of equations. If the system does not have exactly one solution, state whether it has no solution or infinitely many solutions. (Use the following examples to guide you).

```
Example 1: use substitution to solve they system
                                                         Example 2: Solve for one variable, then
of equations.
                                                         substitute.
y = 2x
                                                          x + 3y = 7
4x - y = -4
                                                         2x - 4y = -6
Substitute 2x for y in the second equation.
                                                         Solve the first equation for x since the coefficient
4x - y = -4 second equation
4x - 2x = -4
               y = 2x
                                                             x + 3y = 7
                                                                                First equation
    2x = -4 combine like terms
                                                         x + 3y - 3y = 7 - 3y
                                                                               Subtract 3y from each side
      x = -2 Divide each side by 2
                                                                 x = 7 - 3y
                                                                               Simplify
                and simplify.
                                                         Find the value of y by substituting 7 - 3y for x in
                                                         the second equation.
Use y = 2x to find the value of y.
                                                              2x - 4y = -6 Second equation
y = 2x First equation
                                                         2(7-3y)-4y=-6 x=7-3y
                                                         14 - 6 y - 4y = -6
Distributive Property
14 - 10y = -6
Combine like terms.
y = 2(-2)
               x = -2
y = -4
               simplify
The solution is (-2,-4).
                                                         14 - 10y - 14 = -6 -14 Subtract 14 from each
                                                                               side.
                                                                -10y = -20
                                                                                Simplify.
                                                                    y = 2
                                                                               Divide each side by -10 and
                                                                                simplify.
                                                        Use y = 2 to find the value of x.
                                                        x = 7 - 3y
                                                        x = 7 - 3(2)
                                                        x=1
                                                         The solution is (1, 2).
```

17. 
$$\begin{cases} y = 4x \\ 3x - y = 1 \end{cases}$$

Use elimination to solve each system of equations. If the system does not have exactly one solution, state whether it has no solution or infinitely many solutions. (Use the following examples to guide you).



**18.** 
$$\begin{cases} x + y = -4 \\ x - y = 2 \end{cases}$$

**Find each product.** (Use the following examples to guide you).

Example 1: Find 
$$-3x^2$$
 ( $4x^2 + 6x - 8$ ).

 $-3x^2$  ( $4x^2 + 6x - 8$ )

 $= -3x^2$  ( $4x^2 + 6x - 8$ )

 $= -12x^4 + (-18x^3) - (-24x^2)$ 
 $= -12x^4 - 18x^3 + 24x^2$ 

Example 2: Simplify  $-2(4x^2 + 5x) - x(x^2 + 6x)$ 
 $-2(4x^2 + 5x) - x(x^2 + 6x)$ 
 $= -2(4x^2 + 5x) -$ 

19. 
$$x(5x + x^2)$$

**20.** 
$$-2g(g^2-2g+2)$$

**Factor each polynomial.** (Use the following examples to guide you).

```
Example 1: Use GCF to factor 12mn + 80m²
                                                            Example 2: Factor bax + 3ay + 2bx + by
Find the GCF of 12mn and 80m2
                                                             by grouping.
12mn = 2. 2. 3. m . n
                                                              6ax + 3ay + 2bx + by
80 m2 = 2 · 2 · 2 · 2 · 5 m · m
                                                            = (6ax + 3ay) + (2bx + by)
GCF = 2 - 2 - m or 4m
                                                            = 3a (2x + y) + b (2x + y)
Write each term as the product of the GCF and its
                                                           = (3a + b)(2x + y)
remaining factors.
12mn + 80m^2 = 4m (3 \cdot n) + 4m (2 \cdot 2 \cdot 5 \cdot m)
                                                           Check using the FOIL method.
              = 4m (3n) + 4m (20m)
                                                           (3a + b)(2x + y)
              = 4m (3n + 20 m)
                                                           = 3a(2x) + (3a)(y) + (b)(2x) + (b)(y)
12mn + 80m2 = 4m (3n + 20 m)
                                                           = 6ax + 3ay + 2bx + by
```

**21.** 
$$24x + 48y$$

**22.** 
$$9x^2 - 3x$$

23. 
$$14c^3 - 42c^5 - 49c^4$$

Find each product. (Use the following examples to guide you).

Example 1: Find 
$$(x + 3)(x - 4)$$
 $(x + 3)(x - 4)$ 
 $= x(x - 4) + 3(x - 4)$ 
 $= (x)(x) + x(-4) + 3(x) + 3(-4)$ 
 $= x^2 - 4x + 3x - 12$ 
 $= x^2 - x - 12$ 

Example 2: Find  $(x - 2)(x + 5)$  using FOIL method.

 $(x - 2)(x + 5)$ 

First Outer Inner Last

 $= (x)(x) + (x)(5) + (-2)(x) + (-2)(5)$ 
 $= x^2 + 5x + (-2x) - 10$ 
 $= x^2 + 3x - 10$ 

**24.** 
$$(x + 2)(x + 3)$$

**25.** 
$$(p-4)(p+2)$$

**26.** 
$$(3n-4)(3n-4)$$

**Factor each trinomial.** (Use the following examples to guide you).

### Example 1: Factor each trinomial.

a. 
$$x^2 + 7x + 10$$

In this trinomial, b = 7 and c = 10

Factors of 10	Sum of Factors
1,10	11
2.5	7

b. 
$$x^2 - 8x + 7$$
  
In this trin

In this trinomial, b = -8 and c = 7. Notice that m + n is negative and mn is positive, so m and n are both negative. Since -7 + (-1) = -8 and (-7)(-1) = 7, m = -7 and n = -1.

$$x^2 - 8x + 7 = (x - 7)(x - 1)$$

Example 2: Factor x2 + 6x - 16

In this trinomial, b = 6 and c = -16. This means m + n is positive and mn is negative. Make a list of the factors of -16, where one factor of each pair is positive.

Factors of -16	Sum of Factors
1, -16	-15
-1 , 16	15
2,-8	-6
-2,8	6

Therefore, 
$$m = -2$$
 and  $n = 8$ .  
 $x^2 + 6x - 16 = (x - 2)(x + 8)$ 

**27.** 
$$x^2 + 4x + 3$$

**29.** 
$$c^2 - 4c - 12$$

31. 
$$x^2 - 2x - 3$$

28. 
$$x^2 - x - 6$$

30. 
$$x^2 + 6x + 5$$

Factor each trinomial, if possible. If the trinomial cannot be factored using integers, write "Prime". (Use the following examples to guide you).

Example 1: Factor 2x2 +15x +18.

In this example, a=2, b=15, and c=18. You need to find two numbers whose sum is 15 and whose product is  $2\cdot 18$  or 36. Make a list of the factors of 36 and look for the pair of factors whose sum is 15.

Factors of 36	Sum of Factors	
1, 36	37	
2 , 18	20	
3,12	15	

Use the pattern  $ax^2 + mx + nx + c$  with a= 2, m= 3, n= 12 and c= 18.

$$2x^{2} +15x +18 = 2x^{2} +3x + 12x +18$$
  
=  $(2x^{2} +3x) + (12x +18)$   
=  $x(2x + 3) + 6(2x + 3)$   
=  $(x + 6)(2x + 3)$ 

Example 2: Factor 3x2 - 3x - 18

Note that the GCF of the terms  $3x^2$ , 3x, and 18 is 3. First factor out this GCF.

$$3x^2 - 3x - 18 = 3(x^2 - x - 6)$$

Now factor  $x^2 - x - 6$ . Since a = 1, find the two

tactors	ot	-6	whose	sum	is	-1.
r ,	-	-		,	_	-

Factors of -6	Sum of Factors
1, -6	-5
-1, 6	5
-2,3	í
2,-3	-1

Now use the pattern (x + m)(x + n) with m = 2 and n = -3

$$x^2 - x - 6 = (x + 2)(x - 3)$$
.

The complete factorization is

$$3x^2 - 3x - 18 = 3(x + 2)(x - 3)$$

32. 
$$2x^2 - 3x - 2$$

33. 
$$6x^2 + 5x - 6$$

34. 
$$2a^2 + 5a + 3$$

## Express the following in simplest radical form.

An expression under a radical sign is in simplest radical form when:

- There is no integer under the radical sign with a perfect square factor.
- There are no fractions under the radical sign.
- There are no radicals in the denominator.

35. 
$$\sqrt{50}$$

37. 
$$\sqrt{\frac{6}{27}}$$

**36.** 
$$\sqrt{169}$$

Simplify each exponential expression using the properties of exponents in the table below. Answers should be written using positive exponents.

PROPERTY	
Product of Powers	$a^m \cdot a^n = a^{m+n}$
Power of a Power	$(a^m)^n = a^{m \cdot n}$
Power of a Product	$(ab)^m = a^m b^m$
Negative Power	$a^{-n} = \frac{1}{a^n} \qquad (a \neq 0)$
Zero Power	$a^0 = 1$ $(a \neq 0)$
Quotient of Powers	$\frac{a^m}{a^n} = a^{m-n}  (a \neq 0)$
Power of Quotient	$\left(\frac{a}{b}\right)^m = \frac{a^m}{b^m}$ $(b \neq 0)$

38. 
$$w^{-7}$$

39. 
$$(b^6)^3$$

**40.** 
$$\left(\frac{4x^9}{12x^4}\right)^3$$

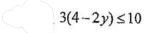
Evaluate the expression for the given value(s).

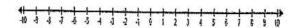
**41.** 
$$\frac{(x+y)^2}{-y}$$
 for  $x = -12$ ,  $y = 4$ 

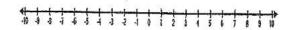
Solve each linear inequality for the given variable and then graph the solution on the number line.

$$a+4 < -a+2$$

#### 43







# **Additional Practice**

**Solving Equations** 

1. 
$$w - \frac{1}{2} = \frac{5}{8}$$

2. 
$$\frac{h}{3} = -2$$

3. 
$$\frac{1}{8}m = 6$$

**4.** 
$$3h = -42$$

5. 
$$-\frac{1}{2}m = 16$$

**6.** 
$$6 - b = 5b + 30$$

7. 
$$5y - 2y = 3y + 2$$

Solving Equations for specific variables

**14.** Solve 
$$ax - b = c$$
 for x.

**15.** Solve 
$$15x + 1 = y$$
 for x.

**16.** Solve 
$$xy + z = 9$$
 for y.

8. 
$$4n - 8 = 3n + 2$$

9. 
$$1.2x + 4.3 = 2.1 - x$$

$$10.\,\frac{1}{2}b + 4 = \frac{1}{8}b + 88$$

**11.** 
$$\frac{3}{4}k - 5 = \frac{1}{4}k - 1$$

**12.** 
$$-3(x+5) = 3(x-1)$$

**13.** 
$$2(y+3t) = -t$$

**17.** Solve 
$$x(4 - k) = p$$
 for k.

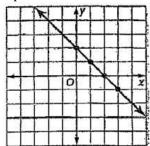
**18.** Solve 
$$xy + xz = 6 + a$$
 for x.

Writing Linear Equations

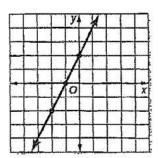
19. Write an equation for the function in function notation and then complete the table.

Х	-1	0	1	2	3
У	-2	2	6		

**20.** Write an equation for each line in function notation.

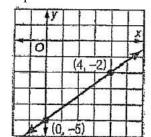


a.

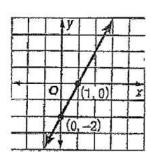


b.

- **21.** Write an equation of the line in standard form given that slope is -2 and the line contains the point (5, 3).
- **22.** Write an equation of the line in standard form given that slope is -1 and the y-intercept is -7.
- 23. Write an equation of the line in standard form that represents each graph.



a.



b.

Graphing Linear Equations and Systems of Linear Equations

**24.** Graph each equation.

a. 
$$3x + y = 2$$

b. 
$$x + y = -1$$

**25.** Graph each system of equations. Determine whether the system has no solution, one solution, or infinitely many solutions. If the system has one solution, tell what it is.

a. 
$$\begin{cases} x = 2 \\ 2x + y = 1 \end{cases}$$

c. 
$$\begin{cases} 3x + 2y = 6 \\ 3x + 2y = -4 \end{cases}$$

b. 
$$\begin{cases} y = \frac{1}{2}x \\ x + y = 3 \end{cases}$$

d. 
$$\begin{cases} 2y = -4x + 4 \\ y = -2x + 2 \end{cases}$$

Solving Systems of Linear Equations

**26.** Solve each system of linear equations using substitution.

a. 
$$\begin{cases} x = 2y \\ y = x - 2 \end{cases}$$

b. 
$$\begin{cases} x = 2y - 3 \\ x = 2y + 4 \end{cases}$$

**27.** Solve each system of linear equations using elimination.

a. 
$$\begin{cases} 2m - 3n = 14 \\ m + 3n = -11 \end{cases}$$

b. 
$$\begin{cases} 3a - b = -9 \\ -3a - 2b = 0 \end{cases}$$

Multiplying Polynomials – find each product.

**28.** 
$$x(4x^2 + 3x + 2)$$

**29.** 
$$-2xy(2y+4x^2)$$

**30.** 
$$3x(x^4 + x^3 + x^2)$$

31. 
$$-4x(2x^3 - 2x + 3)$$

**Factoring Polynomials** 

32. 
$$30mn^2 + m^2n - 6n$$

33. 
$$q^4 - 18q^3 + 22q$$

$$34.4m + 6n - 8mn$$

35. 
$$45s^3 - 15s^2$$

**36.** 
$$55p^2 - 11p^4 + 44p^5$$

37. 
$$14y^3 - 28y^2 + y$$

Find each Product

38. 
$$(x-4)(x+1)$$

**40.** 
$$(y + 5)(y + 2)$$

**42.** 
$$(8m-2)(8m+2)$$

**39.** 
$$(x-6)(x-2)$$

**41.** 
$$(2x-1)(x+5)$$

43. 
$$(k+4)(5k-1)$$

Factor each Trinomial (if not possible, write "Prime)

**44.** 
$$m^2 + 12m + 32$$

**50.** 
$$a^2 + 8a - 9$$

**56.** 
$$3x^2 + 2x - 8$$

**45.** 
$$r^2 - 3r + 2$$

**51.** 
$$y^2 - 7y - 8$$

57. 
$$18x^2 - 27x - 5$$

**46.** 
$$x^2 - 4x - 21$$

**52.** 
$$y^2 + 14y + 20$$

**58.** 
$$18v^2 + 9v - 5$$

**47.** 
$$x^2 - 22x + 121$$

53. 
$$m^2 + 9m + 20$$

**59.** 
$$-4c^2 + 19c - 21$$

**48.** 
$$p^2 - 16p + 64$$

**54.** 
$$3m^2 - 8m - 3$$

**49.** 9 – 
$$10x + x^2$$

55. 
$$16r^2 - 8r + 1$$

Simplifying Radicals

**60.** 
$$\sqrt{24}$$

**61.** 
$$\sqrt{192}$$

**62.** 
$$\sqrt{147}$$

63. 
$$\sqrt{\frac{13}{49}}$$

**64.** 
$$\frac{3}{\sqrt{6}}$$

Simplify each Expression

**65.** 
$$g^5 \cdot g^{11}$$

**66.** 
$$(3x^7)(-5x^3)$$

67. 
$$\frac{-15x^7}{25x^9}$$

68. 
$$\frac{y^{12}}{y^8}$$

**69.** 
$$(-4a^5b^0c)^2$$

Evaluate each expression for the given value.

**70.** 
$$10(t^2 + t)$$
 for  $t = -5$ 

71. 
$$-5|k+1|$$
 for  $k=-10$